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Tatyasaheb Kore Institute of Engineering & Technology, Warananagar
(An Autonomous Institute)

F.Y. B. Tech (Sem-I), In Semester Examination –I, September 2023

ENGINEERING MATHEMATICS-I

Day and Date: Tuesday, 03 September 2023

Marks: 30

Time : 9:15 am to 10:15 am

Instructions: i) Use of non programmable calculator is allowed.
ii) Figures to the right indicate full marks.

Q.1 Attempt any Three from the following questions.

Unit CO
No

- a) Reduce the following matrix to normal form and hence find its rank

$$\begin{bmatrix} 2 & -5 & 3 & 4 \\ 1 & 3 & 5 & 2 \\ 4 & -10 & 6 & 8 \\ 3 & 9 & 15 & 6 \end{bmatrix}$$

1 1 5

- b) Solve the equations by matrix method

$$x + y + z = 3, x + 2y + 3z = 4, x + 4y + 9z = 6$$

1 1 5

- c) Solve

$$2x - y + 3z = 0, 3x + 2y + z = 0, x - 4y + 5z = 0$$

1 1 5

- d) Investigate for what value of *a* and *b* the equations

$$x + y + z = 6, x + 2y + 3z = 10, x + 2y + az = b$$

1 1 5

Have

- i) No solution
ii) A unique solution

Q.2 Attempt any Three from the following questions.

- a) Find the Eigen values and Eigen vector corresponding to largest eigen value of

$$\begin{bmatrix} 7 & -2 & 0 \\ -2 & 6 & -2 \\ 0 & -2 & 5 \end{bmatrix}$$

2 2 5

- b) Find the Eigen values of *A*, *A*², 5*A* for the matrix

$$\begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}$$

2 2 5

- c) Find the Eigen values of *A*, *A*⁻¹, *A*^T for the matrix

$$\begin{bmatrix} 1 & 0 & -1 \\ 1 & 2 & 1 \\ 2 & 2 & 3 \end{bmatrix}$$

2 2 5

- d) Verify Cayley-Hamilton Theorem for matrix *A*

$$\begin{bmatrix} 1 & 2 & 3 \\ 2 & -1 & 4 \\ 3 & 1 & -1 \end{bmatrix}$$

2 2 5

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